

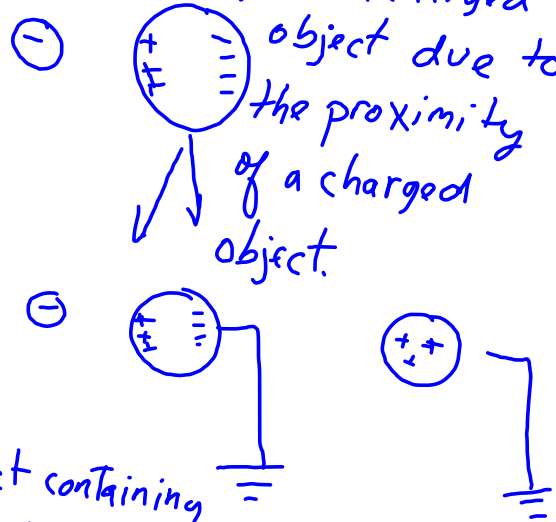
# Electro Statics

- Electric charge — property of matter that allows it to be accelerated by an electric force
- two types: positive (+)  
negative (-)
- Total charge in a closed system is conserved  
(charge cannot be created or destroyed)
- quantized.  
(multiple of  $e$   
charge on electron)

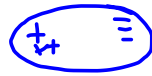
Conductors — materials in which charges move freely (metals)

insulators — materials in which charges do not move freely (non-metals)

Induction — The charging of an uncharged object due to the proximity of a charged object.



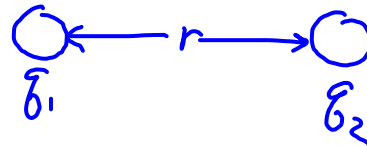
Dipole — object containing two electric "poles"



Polarization — the induced separation of charges (creation of a dipole) in an electrically neutral object.

## Coulomb's Law

$$F = \frac{k q_1 q_2}{r^2}$$



$$k = 8.99 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2} \quad k = \frac{F r^2}{q^2}$$

C = Coulomb = unit of charge

Charge on electron =  $1.6 \times 10^{-19} \text{ C}$

Q. Force between two charges is  $F$ .  
If the separation between the charges is doubled, what is the new force between the charges?

$$A. F = \frac{k q_1 q_2}{r^2}$$

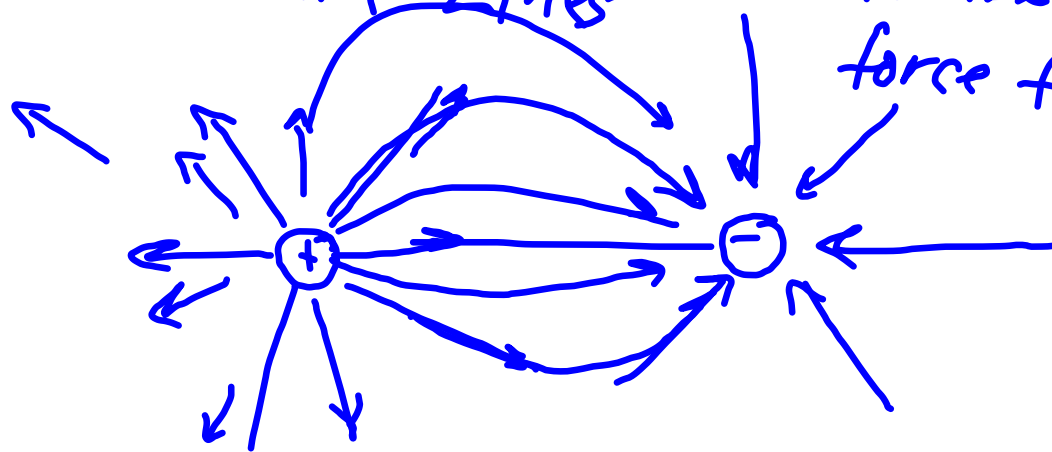
$$F_{\text{new}} = \frac{k q_1 q_2}{r_{\text{new}}^2} = \frac{k q_1 q_2}{(2r)^2} = \frac{k q_1 q_2}{4 r^2} = \frac{1}{4} F$$

Electric Field = Force per charge

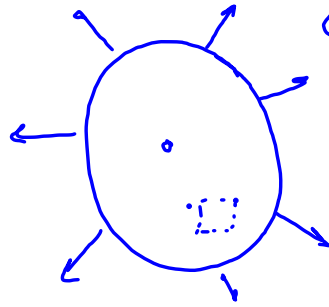


$$E = \frac{F}{q_2} = k \frac{q_1}{r^2}$$
A hand-drawn diagram of a positive charge, represented by a circle with a plus sign inside, and the label  $q_2$  written below it. An arrow points from the charge towards the equation.

Electric Field Lines describe electric force field



Gauss' Laws - Given the electric field at each point of a closed surface, it is possible to determine the net charge within the surface.



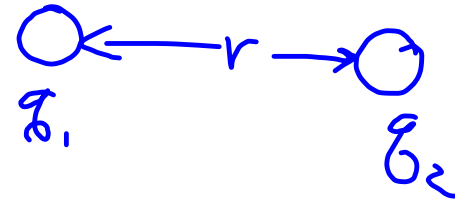
Electric flux -  $E \Delta A$   
↑ electric field  
↑ area through which electric field passes

$$\sum E_{\perp} \Delta A = 4\pi k Q_{\text{enclosed}}$$

↑  
Gauss' Law

# Potential Energy between charges

$$U = \frac{k q_1 q_2}{r}$$



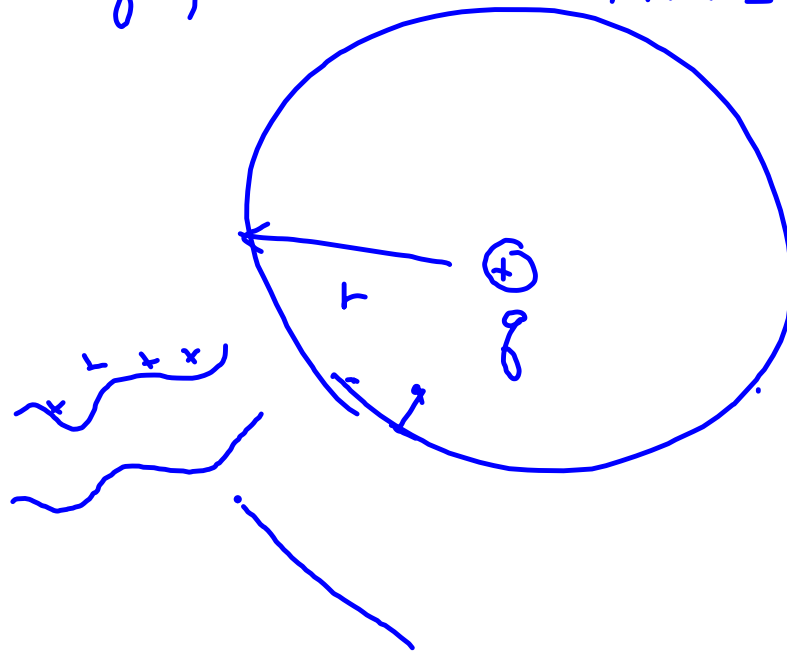
$$V = \frac{U}{q_2} = \frac{k q_1}{r} = \text{Potential Energy per charge due to charge } q_1$$

= "potential"

"potential" = potential energy per charge

$$\text{unit of potential} = \text{volt} = \frac{\text{Joule}}{\text{Coulomb}}$$

# Equipotential Surfaces

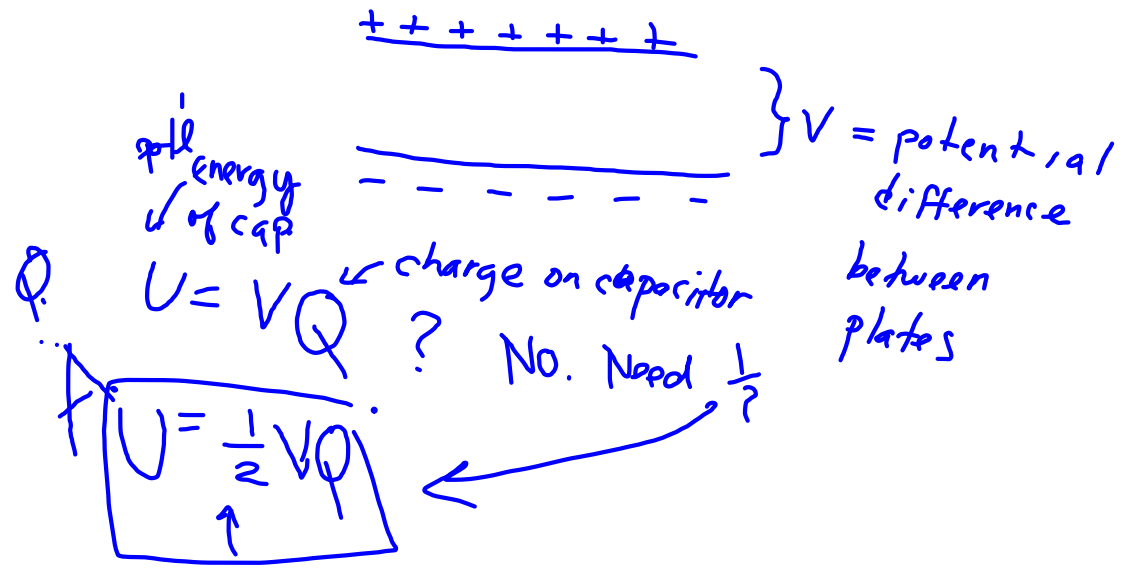


$$V = \frac{kq}{r}$$

A graph showing the relationship between potential  $V$  and distance  $r$ . The vertical axis is labeled  $V$  and the horizontal axis is labeled  $r$ . The graph shows two hyperbolic curves, one in the upper right quadrant and one in the lower right quadrant, both approaching the  $r$ -axis as  $r$  increases. The upper curve represents the potential of a positive charge, and the lower curve represents the potential of a negative charge.

- Electric field lines are perpendicular to equipotential surfaces.
- When a particle moves on a equipotential surface, its potential energy is unchanged.

Capacitor - circuit element that stores electric charge

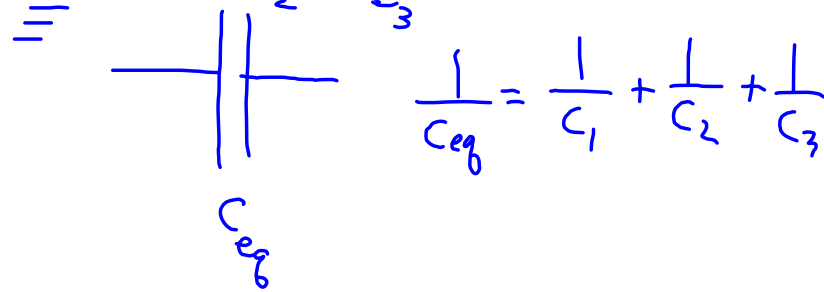
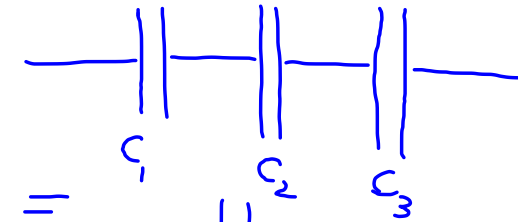


$$C = \frac{Q}{V} = \text{def of capacitance}$$

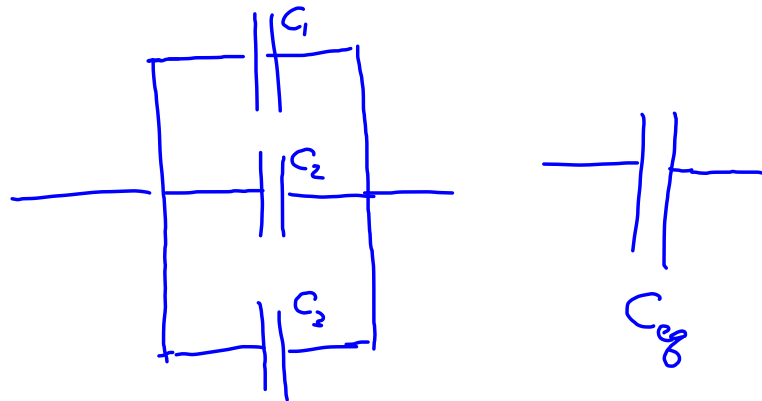
$$U = \frac{1}{2} CV^2 = \text{energy required to charge a capacitor (with capacitance } C) \text{ to voltage } V$$



## Capacitors in Series



## Capacitors in parallel



$$C_{eq} = C_1 + C_2 + C_3$$